

- (a) Let the distance between the disks be  $l$ , where  $l \ll R$ . Since  $Q = It$ , we have, by Gauss Law,

$$E = \frac{It}{\pi R^2 \epsilon_0},$$

with direction pointing from the positively charged plate to the negatively charged one. From

$$\vec{\nabla} \times \vec{B} = \mu_0 \epsilon_0 \frac{\partial \vec{E}}{\partial t},$$

$$B \cdot 2\pi s = \mu_0 \epsilon_0 \frac{I}{\pi R^2 \epsilon_0} \pi s^2,$$

i.e., 
$$B = \frac{\mu_0 I s}{2\pi R^2}.$$

The direction of the B-field is tangential and clockwise when viewed along the direction of the E-field.

(b) Energy density = 
$$\frac{1}{2} \epsilon_0 |\vec{E}|^2 + \frac{1}{2\mu_0} |\vec{B}|^2$$

$$= \frac{I^2 (4t^2 + \mu_0 \epsilon_0 s^2)}{8\epsilon_0 \pi^2 R^4}.$$

Poynting vector 
$$\vec{S} = \frac{1}{\mu_0} \vec{E} \times \vec{B}.$$

i.e., 
$$|\vec{S}| = \frac{I^2 s t}{2\epsilon_0 \pi^2 R^4}.$$

The Poynting vector is pointing inward in the radial direction.

- (c) Total energy

$$U = \iiint_V \left[ \frac{1}{2} \epsilon_0 |\vec{E}|^2 + \frac{1}{2\mu_0} |\vec{B}|^2 \right] dV$$

$$= \int_0^R \frac{I^2 (4t^2 + \mu_0 \epsilon_0 s^2)}{8\epsilon_0 \pi^2 R^4} 2\pi s l ds$$

$$= \frac{I^2 l}{12\epsilon_0 \pi R^2} [6t^2 + \mu_0 \epsilon_0 R].$$

Total power flowing into the gap

$$P = - \oiint_A \vec{S} \cdot \vec{da}$$

$$= \frac{I^2 s t}{2\epsilon_0 \pi^2 R^4} \times 2\pi R l$$

$$= \frac{I^2 l t}{\epsilon_0 \pi R^2}$$

$$= \frac{dU}{dt}.$$